1. What is herd immunity?

   enough ppl immune in a population such that virus runs out of places to spread

2. Define $R_0$ to be the number of people, on average, who will be infected by a single infected person. Note that $R_0$ is pronounced “R naught.”

   If an infected person encounters 10 other people, a virus with $R_0 = 2$ would infect 2 of them, on average.

3. Consider an illness where people who are infected later recover, and they are at that point immune to future infections. Over time, how would $R_0$ change for this ailment?

   $R_0$ gets smaller

   less ppl get infected over time
4. Suppose that a vaccine offers complete immunity. If 5 out of every 10 people take the vaccine, how would that change $R_0$ in the above example? $R_0 = \frac{2}{10} \times \frac{5}{10} = \frac{10}{100} = \frac{1}{10}$

$$R_0 = 1$$

5. Consider an ailment with $R_0 > 4$. Describe what will happen if the community has no vaccines and cannot otherwise protect itself.

community keeps getting sick exponentially

6. Now consider an ailment with $R_0 < 1$. What happens this time?

illness spreads slower over time, but never stops

7. Herd immunity takes hold when enough people are immune such that the effective value of $R_0$ is below 1. Can you calculate the required percentage?

Define $N$ to be the average number of people with whom an infected person comes in contact. In the prior examples, $N$ was 10.

Define $V$ to be the number of vaccinated people in each group of $N$.

Define $R$ to be the number of people in each group of $N$ people who would be infected but for the vaccine.

What value of $V$ will cause the effective rate of infection to drop to 1?

$$V = \frac{N}{R} = \frac{10}{2} = 5$$
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\frac{R}{N} \cdot \frac{N-V}{N} = \frac{1}{N}
\]

\[
R \cdot \frac{N-V}{N} = 1
\]

\[
\frac{N-V}{N} = \frac{1}{R}
\]

\[
N-V = \frac{N}{R}
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\[
\frac{N-N}{R} = V
\]

\[
V = N \left(1 - \frac{1}{R}\right)
\]
8. Should we expect the herd immunity threshold to vary from community to community? Why or why not? Give examples.

9. Suppose that a community has reached herd immunity. What factors might cause the relevant ailment to start increasing despite the supposed immunity?

10. If we wanted to calculate the real-world herd immunity threshold for Covid-19 in Los Angeles, what data would we need?

11. News accounts report that the Pfizer Covid-19 vaccine is 95% effective. What does that mean exactly? Does it mean that, out of every 100 people given the vaccine, we should expect that 5 will fall ill?

12. Test your understanding using the real numbers. Pfizer recruited 43,661 volunteers for its first large vaccine trial. Half were given the real vaccine and half were given a placebo. After six weeks, 170 had fallen ill with Covid. Out of those 170, 8 had actually received the vaccine. Is this data consistent with the claim that the vaccine is 95% effective?
Last week, the New York Yankees baseball team announced nine cases of Covid-19 in fully vaccinated members of the team organization. Specifically, one player, three coaches, and five staff members tested positive. Assuming that everyone in the Yankees organization was vaccinated with a vaccine that is said to be 75% effective, is this size of a “breakthrough” surprising? Convince me.