

Properties of Series

①

$$\sum c \cdot a_n = c \sum a_n$$

* $c = \text{constant}$



example

$$\sum_{n=1}^8 7 \cdot n = 7 \cdot \sum_{n=1}^8 n$$

↓
[7, 14, 21, 28, 35, 42, 49, 56]

↓
7 · [1, 2, 3, 4, 5, 6, 7, 8]



[7, 14, 21, 28, 35, 42, 49, 56]

②

$$\sum a_n + b_n = \sum a_n + \sum b_n$$



example

$$\sum_{n=1}^4 3n + n^2 = \sum_{n=1}^4 3n + \sum_{n=1}^4 n^2$$

↓
[3, 6, 9, 12, 15]

↓
[1, 4, 9, 16, 25]

↘ ADD ↙

[4, 10, 18, 28, 40]

Homework!

① Solve $\sum_{n=3}^{10} a_n + b_n$

$$a_n = 2^n$$
$$b_n = 3n - 2$$

② Solve $\sum_{n=1}^{10} a_n$

$$a_n = (-1)^n$$

③ Write the following in series notation $\left(\sum_{?}^{?} = ? \right)$
 $10 + 12 + 14 + 16 + 18 + 20$

④ Write the following in series notation $\left(\sum_{?}^{?} = ? \right)$
 $\frac{5}{8} + \frac{5}{9} + \frac{5}{10} + \frac{5}{11} + \dots + \frac{5}{34}$