

- (4) Fill out the following multiplication table (you can either draw pictures; or flip and rotate a model triangle, or multiply permutations).

	$I$	$F_1$	$F_2$	$F_3$	$\circlearrowleft$	$\circlearrowright$
$I$						
$F_1$						
$F_2$						
$F_3$						
$\circlearrowleft$						
$\circlearrowright$						

- (5) Write down as many interesting things about this multiplication table as you can.

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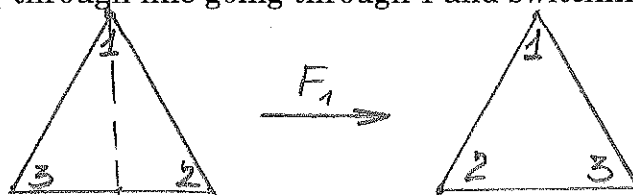
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There are also three flips:

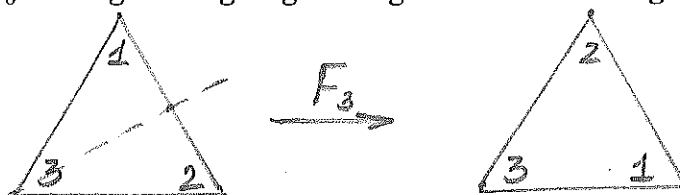
- The flip  $F_1$  through line going through 1 and switching 2 and 3:



- The flip  $F_2$  through line going through 2 and switching 1 and 3:



- The flip  $F_3$  through line going through 3 and switching 1 and 2:



(2) When the triangle is flipped, the vertices also end up in the new places. Write down the permutations corresponding to the clockwise and the counterclockwise rotations:

(a) Flip  $F_1$ :

$$\begin{pmatrix} 1 & 2 & 3 \\ \downarrow & \downarrow & \downarrow \end{pmatrix};$$

(b) Flip  $F_2$ :

$$\begin{pmatrix} 1 & 2 & 3 \\ \downarrow & \downarrow & \downarrow \end{pmatrix};$$

(c) Flip  $F_3$ :

$$\begin{pmatrix} 1 & 2 & 3 \\ \downarrow & \downarrow & \downarrow \end{pmatrix};$$

When no transformation is performed, we get the *identity permutation*:

$$\begin{pmatrix} 1 & 2 & 3 \\ \downarrow & \downarrow & \downarrow \\ 1 & 2 & 3 \end{pmatrix};$$