

- (c) Vague life advice from a Kung fu instructor (You must find inner peace, only then can you hope to perfect the golden flying pan fried monkey technique.)

- (d) Euclid's algorithm that we used to find the greatest common divisor of two numbers.

- (e) An algorithm for writing your first novel (Come up with an interesting premise and characters. Find a compelling conflict, ...)

- (f) What are other examples of algorithms that are not covered above? What about things that aren't algorithms?

In order to first talk about writing our own algorithms, it helps to take a specific example.

Suppose that we have a robot named Dora. Dora lives in a hallway which has two doors (denoted by the letter 'D') which has a tiled floor. On some of the tiles, some birds have made their nests (the birds are funny looking, they look like ♣). Here is an example of what Dora's hallway might look like.



Dora can only understand the following simple instructions:

(a) Move one tile to the right or left.

```
move_left, move_right
```

(b) Check if there is bird nest in the current tile that Dora is in.

```
bird_in_tile
```

(c) Check if Dora has a door on her right/left.

```
door_on_left, door_on_right
```

(d) turn off

```
turn off
```

Dora also knows how to execute a series of command if a statement is true, and how to repeat something. For example, if I wanted to write an algorithm to make Dora move all the way to the left door, then I could write:

```
while (door_on_left = false)
  move_left
turn off
```

Dora can also count, and can store variables, and can do some very basic arithmetic. If I wanted to have Dora move to the end of the hallway, and count how many steps it took and output that number, I could modify the above algorithm to do the following:

```
number_of_steps = 0
while (door_on_left = false)
  move_left
  number_of_steps = number_of_steps + 1
output number_of_steps
turn off
```

2. Now it is your turn to write some algorithms. For the following, assume that Dora starts next to the right door. Also, make sure that Dora turns off after she finished implementing the algorithms!

(a) Have Dora output 'yes' if she finds any nests in the hallway, and 'no' otherwise.

Now that you have an idea of what an algorithm is, and some practice writing your own, let's work on writing some algorithms to do math.

Suppose that you have a function

```
add_one(x)
```

which takes in one input, x , and returns the number $x + 1$, so the following algorithm would output 7

```
a = 6
y = add_one(a)
output y
```

If we have this algorithm, then we get for free an algorithm to add 2 to a number, as follows

```
function add_two(x)
y = add_one(x)
z = add_one(y)
return z
```

The first line in the above function should read: This is a function with the name 'add_two' which takes one input argument, referred to by the name x .

3. Suppose now, that we have a machine that can add or subtract number, and can correctly interpret statements like $A < B$ for integers A and B . For all of these problems, I encourage you to use functions that you have written before when you are writing new functions!
 - (a) Write a function called 'multiply(x,y)' which takes in two arguments, x and y , and returns x times y .
 - (b) Write a function called 'exponentiate(x,y)' which takes in two arguments, x and y , and returns x^y .
 - (c) Write a function called 'mod(x,y)' which takes in two arguments, x and y , and returns x modulo y . For example, $mod(4,7)$ should return 4, $mod(13,4)$ should return 1, etc.
 - (d) Write a function called 'divide(x,y)' which takes in two arguments, x and y , and returns x/y . You can assume that
 - (e) Write a function called 'gcd(x,y)' which takes in two arguments, x and y , and returns the greatest common divisor of x and y .
 - (f) Write a function called 'isPrime(x)' which takes in one argument, x and returns true if x is prime, and false otherwise.
4. Just in case you are bored, or looking for something else to do, here are some more cryptograms, which use substitution cyphers. Remember, the longer a cryptogram is, the easier it is to break! Hint, both of these are from the same scene, in the same movie.

(a) DPI'R MSCU OP OQSAC OQGO, JPIMRA'O DPI? DPI'BU FU-
GOUA LD NSGAO, JQSEQ LUGAV DPI'KU UHEUTOSPAGMMD
VOKPAN, VP DPI EPIMR'BU TIO OQU TPSVPA SA DPIK PJA
NPFMUO, OKIVOSAN PA DPIK VOKUANOQ OP VGBU DPI,
VP S EGA EMUGKMD APO EQPPVU OQU JSAU SA XKPAO
PX DPI. FIO, DPI'BU GMVP FUVOUR LD VTGASGKR, JQSEQ
LUGAV DPI LIVO QGBU VOIRSUR, GAR SA VOIRDSAN DPI
LIVO QGBU MUGKAUR OQGO LGA SV LPKOGM, VP DPI
JPIMR QGBU TIO OQU TPSVPA GV XGK XKPL DPIKVUMX
GV TPVVSEFMU, VP S EGA EMUGKMD APO EQPPVU OQU
JSAU SA XKPAO PX LU.

(b) NWO'U SLAR MW MCLGA MCDM, YWOSUG'M NWO? NWO'BR
QRDMRG VN ELDGM, YCLHC VRDGF NWO'PR RIHRKML-
WGDSSN FMPWGE, FW NWO HWOSU'BR KOM MCR KWLFWG
LG NWOP WYG EWQSRM, MPOFMLGE WG NWOP FMPRGEMC
MW FDBR NWO, FW L HDG HSRDPSN GWM HCWWFR MCR
YLGR LG XPWGM WX NWO. QOM, NWO'BR DSFW QRFRU
VN FKDGLDPU, YCLHC VRDGF NWO VOFM CDBR FMOULRU,
DGU LG FMOUNLGE NWO VOFM CDBR SRDPGRU MCDM
VDG LF VWPMD, FW NWO YWOSU CDBR KOM MCR KWLFWG
DF XDP XPWV NWOPFRSX DF KWFFLQSR, FW L HDG HSRDPSN
GWM HCWWFR MCR YLGR LG XPWGM WX VR.